# Beyond the displacement cascade: nanostructural evolution in metals under irradiation and correlation with mechanical properties

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# Outline

## Introduction

# Part I – Nanoscopic scale

- Production of damage
- Development of a nanostructure
- Microchemistry
- *The set of the set of* 
  - Atomistic Monte Carlo
  - Coarse grained models

# Part II – Mesoscopic scale and beyond

- Dislocations and hardening
- How to model this:
  - Dislocation dynamics
- Ideas about multiscale modelling



# Introduction: why do we study and model radiation damage?







#### Hardening: yield strength increase











# How does irradiation change the macroscopic properties of steels

# To understand this we need to see what radiation does at the proper scales involved ...



# Part I: Nanoscopic scale





## Production of damage: the displacement cascade







#### ... It all starts with a neutron hitting an atom ...

Neutrons = uncharged particles  $\Rightarrow$  can travel long distances in matter When reacting with nuclei of atoms they can produce

- Activation
- Transmutation (He, H)
- Displacement damage (elastic collisions)



# Displacement cascade: the mother of all evils ...







#### A closer look at the cascade phases



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## **Primary state of damage**





## What happens next? Development of a nanostructure







# **Clustering of point defects**

- Clusters of vacancies
  - 🖙 nano-cavities
  - vacancy dislocation loops
- Clusters of self-interstitials
  *interstitial dislocation loops*



[110] dumbbell

Stable in Fe if isolated or in small clusters



[111] dumbbell or crowdion

Unstable in Fe if isolated but unit of large clusters









## Self-interstitial loops ('prismatic loops')



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#### **Stacking-fault tetrahedra**



#### **3D result**









Schaublin et al., Phil. Mag., 2005





#### Defect migration and cluster growth SIA clusters



SIA clusters migrate fast in 1D





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#### Defect migration and cluster growth Vacancy clusters





Vacancy clusters migrate slowly in 3D – can coalesce













#### **Evidence of point-defect cluster growth**



Loops in 150 keV Fe<sup>+</sup> irradiated ultra-high-pure Fe at 300°C

Courtesy of M. Hernández Mayoral



Cavities (above) & Frank loops (below) in irradiated 316 SS at high T



Garner & Gelles, JNM 159 (1988) 286





#### **Defect recombination and disappearance at sinks**





Does everyone know what a dislocation and a grain boundary are?



## Take home messages

- Either by diffusion or directly in displacement cascades, point-defects tend to join to form clusters
  - Vacancies: cavities, loops, other (stacking fault tetrahedra)
  - SIAs: loops only

> SIA clusters migrate fast in 1D and are highly stable

Vac. clusters migrate slowly in 3D and dissolve above stage V (if not stabilised by something)

Migrating defects eventually recombine or disappear at sinks

*Tisible defects are there because they do not move* 



## What happens next? Microchemical changes







#### **Transport of chemical species**



If stable, mixed dumbbell transports solutes to sinks





#### **Competition between chemical species**







### Typical example: radiation-induced segregation

#### **Observed in <u>austenitic steels</u>**

Determines higher susceptivity to stress corrosion cracking

Irradiation Dose Effects on Cr Grain Boundary Composition Profile

#### Irradiation Dose Effects on Si Grain Boundary Composition Profile

Heat

316-2

8

12

GΒ





# Radiation-enhanced and radiation-induced

#### **Enhanced**





Precipitates form because higher number of point defects under irradiation enhances transport and accelerates their formation

<u>They would form also under</u> <u>high T annealing</u> Precipitates form because continuous flux of point defects to sink increases local solute concentration, until solubility limit is locally exceeded

This would not happen without irradiation





### Phases of precipitation Nucleation, Growth and Coarsening





(b)

(c)



(a)



#### **Example of radiation-enhanced phenomena**

#### **Cu-rich precipitate formation in RPV steels**



#### Cu-free Ni-Mn-rich precipitate formation in RPV steels: radiation-enhanced or radiation-induced?



Konobeev et al., JNM, 2006

Cr-rich precipitate formation in high-Cr steels





#### Summary: Nanostructural evolution under irradiation

Dislocation

#### Point defect evolution



Nucleation, growth and coarsening of dislocation loops



Nagai et al.,

Radiation induced segregation at sinks (grain boundaries, dislocations, ...)

Microchemical evolution





Nucleation, growth & coarsening of voids



Radiation enhanced/induced precipitation



#### How do we model these processes? Atomic-level modelling: Molecular dynamics







# **Molecular Dynamics**

#### Principle

The classical equations of motion for a set of N atoms are timestepwise solved, using finite difference integration algorithms, so as to know atomic positions and velocities at each timestep:

$$m\frac{d^2\bar{r}_i}{dt^2} = -\nabla V(\bar{r}_1, \bar{r}_2, ..., \bar{r}_N) \quad \rightarrow \quad \{\bar{r}_i, \bar{v}_i / i = 1, ..., N\}$$

- From the knowledge of atomic positions and momenta all statistical mechanics magnitudes are directly accessible
- The <u>core of the method</u>, containing all the physics, is the <u>interatomic potential</u>, V(r<sub>i</sub>), from which the interatomic forces are derived



## **Applications of MD for irradiation problems**

- MD is the technique "par excellence" for displacement cascade simulations:
  - one atom is given kinetic energy
  - the dynamic evolution of the system is followed
- MD also allows stability and mobility of (fast enough) defects to be studied
- Finally, MD can be used to model the interaction between dislocations and defects

#### 20 keV cascade (peak time) in Fe









## Pros & Cons of MD

#### Advantages

- Wide applicability (bulk, surfaces, crystals, amorphous, liquids, ...)
- No analytical simplifications or approximations
- Treats spontaneously complex systems and phenomena at equilibrium or far from it, not accessible to analytical approaches

#### Limitations

- Evolution of the system calculated by timesteps of ~1 femtosecond
- Limited timescale (tens of nanoseconds, trade-off size/time)
- Limited volumes (up to 10<sup>7</sup> atoms): not big enough for e.g. extended defects
- All the physics is contained in the interatomic potential



#### How do we model these processes beyond MD scale? Atomic-level modelling: Monte Carlo







## **Stochastic Monte Carlo Algorithms**

- MD cannot deterministically reproduce the evolution of a system to equilibrium if the kinetics is slower than nanoseconds
- MC methods can be used for this purpose or more generally to extend the timespan of radiation damage simulations:
  - Metropolis Monte Carlo
  - Kinetic Monte Carlo
    - ✓ Atomistic KMC
    - ✓ Object KMC





# **The Monte Carlo Algorithm**

> List of possible events:  $e_i / i=1, ..., N_e$ 

> A probability  $P_i$  is associated to each event

 $\succ \Sigma_i P_i = 1$ 




# **Metropolis Monte Carlo**

- > System of *N* atoms, defects can be included
- Total energy must be calculable, e.g. using an interatomic potential
- One trial event is chosen between:
  - atomic position exchange
  - small atomic displacement
  - global expansion or contraction
- > If  $E_{after}$   $E_{before} = \Delta E < 0$ , the trial is accepted
- > If  $\Delta E$  > 0, the trial is accepted with probability exp(-  $\Delta E/kT$ ) < 1

(by extracting a random number, which can fall only in one out of two possible probability intervals)





# **Application of Metropolis MC**

Study Cr redistribution in presence of a grain boundary: is segregation favoured or not?

Cr atoms only: {111}



Cr 2D distribution

#### **Cr 3D distribution**





# **Metropolis Monte Carlo**

### Advantages

- Phenomena such as segregation or precipitation, out of scope for MD, can be studied
  - ✓ (given a suitable hamiltonian and on the condition that these correspond to equilibrium states)
- All contributions to the free energy can be included in the calculation
  - Powerful tool to evaluate phase diagrams

Problems:

- Evolution does not involve physical mechanisms, only total energy
- Intermediate configurations are physically not meaningful
- No information is given about time necessary to reach equilibrium





# **Kinetic Monte Carlo**

*Kinetic*  $\Rightarrow$  time is introduced !

Probabilities are calculated for physical transition mechanisms as Boltzmann factor frequencies :

$$\Gamma_i = \nu_i \exp\left(-\frac{E_{a,i}}{kT}\right)$$

After a certain event is chosen, time is in amount:

$$\Delta \tau = \frac{-\ln(rand)}{\sum_{i=1}^{N_e} \Gamma_i} = \frac{1}{\sum_{i=1}^{N_e} \Gamma_i}$$

Most physics (kinetics and thermodynamics) contained in the activation energies !

SCR. CEN

(residence time algorithm)



# **Kinetic Monte Carlo Families**





Atoms (alloy) on rigid lattice Mainly vacancy jumps (SIA in 1st approx.)

Energy parameters from interatomic potentials or DFT

KMC residence time algorithm





"Objects" on *non-atomic* lattice (V, SIA, clusters, ...)

Many possible reactions between "objects"

Large set of parameters covering all possible reactions is needed





### **Example of application of AKMC: precipitation in FeCr**



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### **Difference between AKMC and MMC**





unknown

Final state





Time required is computed





# **AKMC: Pros & Cons**

### Advantages:

- Atomic-level method: can treat diffusion processes including proper atomic level mechanisms
- Can be extended to relatively long timescales (it depends on the problem), much longer than MD any way (seconds easily)

### Limitations:

- Computationally expensive: the volumes that can be simulated remain fairly small
- At the moment, the treatment of SIA is only tentative



### How do we model these processes to their full timescale? Nanostructure evolution models







### **Coarse-grained** microstructure evolution models

### $\succ$ Coarse-grained $\rightarrow$ no atoms

The "elements" or "grains" of the simulation are not atoms:

✓Defects (point-defects, clusters, precipitates) → nanostructure evolution models

✓ Dislocations → dislocation dynamics models

✓ Grain-boundaries  $\rightarrow$  texture models

Nanostructure evolution models for radiation damage are those that in principle allow direct comparison with experiments:

Rate theory

**√**...

Object kinetic Monte Carlo (and similar)





# Nanostructure evolution models: **Rate Theory**

Mean-field approximation:  $\succ$ 

> Defects are created, react and disappear at sinks everywhere at the same rate



- The same thing happens in each infinitesimal volume dV
- Different from periodic boundary
  - $\checkmark$  dV  $\rightarrow$  0 (infinitesimal)
  - There is no real simulation
  - Only variables are concentrations



Reaction

term



# Nanostructure evolution models: Rate Theory

$$A + B \xleftarrow{k_{A+B}^{+}}{k_{C}^{-}} C \quad \frac{\partial C_{B}}{\partial t} = G_{B} + D_{B} \nabla^{2} C_{B} - \left(k_{A+B}^{+} C_{A} C_{B} - k_{C}^{-} C_{C}\right)$$

- N (10s to 100s) coupled differential equations of this type need to be written, one for each defect species
- The actual rate theory concerns the determination of the "rates" at which the reactions occur
  - E.g., through the theory of diffusion-limited reactions and based on mass-action law we know that:

$$k_{A+B}^{+} = 4\pi (r_A + r_B) (D_A + D_B)$$
  $k_C^{-} \propto k_{A+B}^{+} \exp \left(-\frac{E_b}{kT}\right)$ 

- Thus, given the source terms, the basic ingredients of nanostructure evolution models are
  - Diffusion coefficients
  - Capture radii
  - Binding energies





# Nanostructure evolution models: Rate Theory – Pros & Cons

#### Advantages:

- Computationally cheap :
  - Sensitivity studies easily performed
  - Fitting of parameters to experiments is possible
  - Large fluences and volumes are no problem
  - Steady-state or simplified expressions can be analytically obtained
- Fully theoretical framework within which radiation effects can be addressed
  - It is not a "simulation"
  - Computer solves system of eqs.

#### Drawbacks:

- Random inhomogeneities and geometrical effects (e.g. coalescence) not taken into account
- Introduction of new mechanisms requires specific theoretical developments
- All acting mechanisms and parameters must be known
  - The model does not provide them, like e.g. MD
- Atomic-level configurations are not provided, either
  - As compared to e.g. AKMC





### Nanostructure evolution models: Object kinetic Monte Carlo





# Nanostructure evolution models: Object kinetic Monte Carlo

- Volume containing "objects" exists:
  - Point-defects and their clusters
  - Precipitates, solutes, …
  - Traps and localised sinks
  - Dislocations
  - 🐲 (Grain boundaries)
- Each "object" is defined by:
  - 🖙 Туре
  - (centre-of-mass) position
  - Migration parameters
  - Possible reactions
  - Reaction radius
- Events can be
  - Thermally activated → activation energy (migration, emission)
  - *External of known rate P<sub>i</sub> (cascades, ...)*
  - Effect of geometry (recombination, trapping, clustering)

- As for the rate theory, the basic ingredients are
  - Diffusion coefficients
  - Capture radii

æ.

Binding energies





# Nanostructure evolution models: Object kinetic Monte Carlo: Pros & Cons

#### Advantages:

- Flexibility in introducing objects, mechanisms and parameters, taken from any source of information (DFT, MD, AKMC, experiments, ...)
- No theoretical developments required for each new mechanism
- Spatial inhomogeneities and correlations (including sink strengths) are spontaneously accounted for
- Defects behave in a realistic way

#### Drawbacks:

- No atomic configurations
  - As compared to *atomistic* KMC
- All mechanisms and parameters must be known in advance
  - The model does not provide them, like MD does
- Computationally expensive
  - (as compared to rate theory)
  - Small volumes reduce statistical significance, especially for low densities
  - Fitting not possible; sensitivity studies possible, but at high cost



# Part II: Mesoscopic scale and beyond





# **Dislocations and hardening**







### **Dislocations**

**Edge type** 



Dislocation glide under shear is the most frequent mechanism whereby metals are <u>irreversibly deformed</u> (plastic deformation)







clear Materials



### **Dislocations**







FIGURE 1-23. (a) Shear of a perfect crystal to form a mixed dislocation. (b) Projection normal to the glide plane in (a). (c) Resolution of (b) into components at point B.

From Hirth and Lothe, Theory of Dislocations





### **Dislocations, slip planes and deformation**







### Hardening = Yield strength increase







### Why does the yield strength increase after irradiation?



Defect populations act as obstacles for dislocations There are different classes of obstacles ...





# **Shearable obstacles**







### **Shearable obstacles**







# **Shearable (weak) obstacles**



Dislocations can cut through the obstacle: the bigger, the more difficult to cut it through

Elastic, chemical, and phase stability effects also play a role to determine obstacle strength



Increasing strain 'chops up' sheareable obstacles





### Impenetrable obstacles







### Impenetrable obstacles







### **Impenetrable obstacles**



The bigger the spacing between obstacles, the easier for the dislocation to squeeze through the gaps.

Each 'bypass' event leaves a dislocation loop behind, narrowing the gaps and increasing hardening.







# **Prismatic loops are** <u>*absorbable*</u> **obstacles**

This is a peculiar feature of irradiated materials









# Take home messages

- Dislocations are defects that always exist in metals (and other materials) and make irreversible (plastic) deformation possible
  - This is why metals are ductile: they can deform before breaking

The yield strength is the stress to be applied to make dislocations move in a material

➤ The presence of defects (loops, voids, precipitates, ...) from irradiation makes dislocation glide more difficult → the yield strength increases, the material becomes <u>harder</u>



# **Dislocation dynamics**





### **Dislocation dynamics: basics**

In a DD model, a curved and continuum dislocation line is discretised as small segments, e.g. normal to each other (edge/screw)



To refine description, length of segments can be reduced (increase of computational time), or more than two species of segments, including slanted ones with mixed dislocation properties, can be included





# **Dislocation dynamics: basics**

Elements of simulation are dislocation segments that are displaced according to the forces acting on them







# **Dislocation dynamics: basics**

- Elasticity theory provides the background formulation
- Any mechanism that cannot be described in terms of elasticity must be introduced as <u>special local rule</u>
  - **o** e.g. pinning of dislocation by precipitate or radiation defect)






#### MD as tool to study dislocation/defect interaction



Edge dislocation interacting with SIA loop at 600 K





# **Dislocation Dynamics: pros & cons**

Complex dislocation line patterns can be reasonably well predicted



Deformation of a fcc single crystal (Cu) of linear dimension  $15 \mu m$ . The stress tensile axis is [100], the imposed strain rate is 50 per second and the plastic strain reached at the end of this sequence is 0.1%.

Stress-strain curve for single crystal of defined material can be acceptably predicted for small deformations







# **Dislocation Dynamics: pros & cons**

Possible to separate variables and identify mechanisms mainly responsible for given effects



#### Main limitations

- Computationally still very heavy
- No standardized approaches (such as in MD or KMC)
- Limited to single crystals
- No generalized method to introduce irradiation induced defects, though progresses are in course





# Other models at higher scales based on FE (not described here)

#### Crystal plasticity

- Describes how aggregates (portions of polycrystals)
  behave mechanically, given crystalline constitutive laws
- Most immediate way to transfer dislocation dynamics results to finite elements

#### Homogenisation

Allows a single, average constitutive law to be obtained for an aggregate, to be used for larger scale calculations where grains and crystallography are not explicitly treated

#### Reference volume element scale calculations

- RVE is the biggest volume for which the homogenisation is possible without loosing too much information
- Component scale calculations
  - Those used for the design of components, as simple as possible









# What is multiscale modelling?

Use of the proper experimental examination and modelling technique to study each phenomenon of interest <u>at the correct scale</u>

Combination of experimental and modelling techniques to describe phenomena <u>at different scales</u>

Intensive and extensive use of not only advanced theory and experimental techniques, but also, and especially, <u>computer simulation</u>



# Radiation effects are inherently a multiscale problem

1 fs =  $10^{-15}$  s 1-100 ps =  $10^{-12}$   $10^{-10}$  s  $ns = 10^{-9}$  s ....  $ns = 10^{-3}$  s .... 1 s ....  $10^{3}$  s

Time scale







# Main open issues

>Atomistic simulations in multi-component systems

- Possible only with DFT, within size limits
- Interatomic potentials still challenging
- AKMC models possible by paying prices
- Treat in one model microchemical and nanostructural evolution
  - Difficult to treat self-interstitials in AKMC models
  - Difficult to treat chemical complexity in OKMC or RT models
- Bridge between MD and DD
  - Progresses made recently towards a standard approach to transfer information
  - Hampered by non unified standard for DD approaches
- Bridge between discrete and continuum models
  - Especially from DD to crystal plasticity





# Take home messages

The multiscale modelling approach is based on the philosophy of using the right physical technique for the right scale and, if possible, combine them to provide a full physical description of an observed phenomenon

> A number of computer-based modelling techniques exist, e.g.:

- *Atomic-level: molecular dynamics, Metropolis MC, atomistic kinetic MC*
- Nanoscale: rate theory, object kinetic Monte Carlo
- *Microscale: dislocation dynamics*
- Larger scales: finite element methods (from crystal plasticity to component calculations)

The proper use of a multiscale modelling approach, including proper use of advanced experimental techniques, bears the promise to lead to the development of physics-based predictive models



#### The End



